

MODELS AND AN ALGORITHM FOR MULTI-CRITERIA SYNTHESIS OF CONTROL TECHNOLOGIES MANAGING INFORMATION SYSTEMS OF VIRTUAL ENTERPRISES

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ABSTRACT

Integrated information systems (IIS) of virtual enterprises (VE) were considered as objects of control. Two interrelated problems were jointly stated. The first problem lied in program management of IIS and ranking its structural states. The second one implied that control functions regulating business processes should be reallocated among elements and subsystems of IIS in a real time mode. A formal multi-criteria description of these problems was made and a combined (simulation-based) algorithm of a solution was worked out.

INTRODUCTION

Virtual enterprises unite independent multi-business partners (real enterprises) within a temporal task-oriented technical-organizational structure through information technologies and telecommunications (Camarihna-Matos et al. 2004, Wang and Norrie 2001, Ivanov 2003). Virtual enterprises are highly adaptive to consumer needs and benefit juridical and physical persons providing them with dynamic use of common resources during remote collaboration within a business project.

A virtual enterprise is a typical example of a modern integrated transport, production and trading network performing intensive structural dynamics. This issue makes the structural synthesis of a VE more complicated. In particular, the structure dynamics have a complicative influence upon the following tasks: partner selection (producers and suppliers of components,

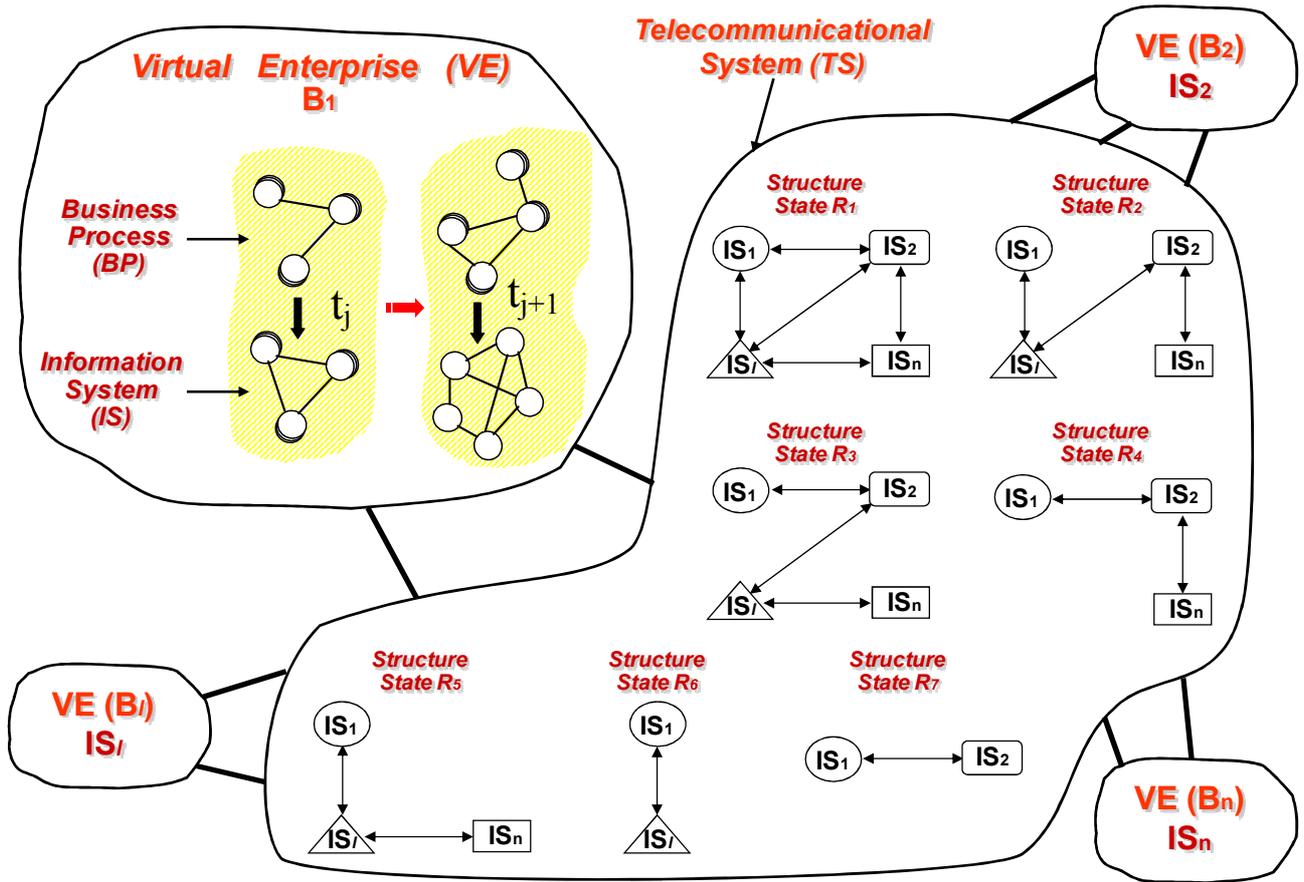
retailers, etc); end products configuring; placement of orders; configuring transport network and information resources (Camarihna-Matos et al. 2004, Wang and Norrie 2001).

An integrated information system is one of the main subsystems of VE. It should be constructed through a real-time configuring (structure-functional synthesis) and interconnection of individual information systems belonging to participants (real enterprises).

It is obvious that IIS run under conditions of structure dynamics same as VE does (Okhtilev et al 2006). Possible variants of structure dynamics involving modern information systems are illustrated in fig. 1. Our previous investigations confirmed that incrementation (stabilization) of IIS potentialities and capacity for work necessitates structures control (including the control of IIS structures reconfiguration). There are many possible variants of structure-dynamics control suitable for IIS. The following variants are the most typical: alteration of IIS functioning means and objectives; controlled motion of CTS elements and subsystems; alteration of the order of IIS tasks; redistribution of functions, tasks, control algorithms and information flows among IIS levels; reconfiguring of degraded structures; flexible use of reduced technologies of IIS control.

As applied to IIS, the structure-dynamics control belongs to the general discipline of structure-functional synthesis and program construction, provided for IIS development (Okhtilev et al 2006, Kalinin and Sokolov 1995, Zvirkun and Akinfiev 1993, Zvirkun et al. 1985, Zimin and Ivanilov 1971).

Here we consider an important problem of structure-dynamics control including interrelated business processes (BP) planning and planning of IIS operations aimed at BP improvements.



Figures 1: Variants of structure dynamics

PROBLEM STATEMENT

Modern IIS ought to reconfigure and adjust information processes in order to agree with changeable business projects and conditions of their execution.

Efficient functioning of IIS necessitates flexible redistribution of tasks, functions and algorithms among elements, subsystems and levels of the system. Therefore following main tasks have to be redistributed: receiving, transmission and processing of information, planning and control of IIS and VE operation. Moreover, different control technologies involve different variants of IIS structures and different information flows in control loops of IIS.

From a formal point of view a selection (synthesis) of BP structure as well as a real-time structure-functional synthesis of IIS implies joint multi-criteria optimization of VE and IIS operation, selection of control functions for business processes and redistribution of control functions among nodes of IIS. Due to the real-time mode of the IIS, the problem to be solved is more complicated than the ones described in the works of (Zvirkun and Akinfiyev 1993, Zvirkun et al. 1985).

The problem of real-time distribution of control functions can be solved at different stages of BP life cycle. In our approach we consider the period of IIS

operation planning with simultaneous preliminary distribution of control functions among main elements of IIS and with construction of control programs for these elements. The control programs can be corrected at the stage of real-time control (implementation of the plan). Program corrections can be accompanied by reallocation of resources and by reconfiguration of IIS structures.

Let us introduce some notation for problem definition. Let $A = \{A_i, i \in N = \{1, \dots, n\}\}$ be a set of business processes (and corresponding control functions) to be implemented at some node of IIS at a given time interval $T = [t_0, t_j]$. To achieve the VE goals during the interval T, the BPs have to be fulfilled. We distinguish between the functions of goal definition, planning (long term and operational planning), real-time control, VE states analysis, external situation analysis and coordination. The set $A = \{A_i, i \in N\}$ is related to sets of informational-technological operations

$D^{(i)} = \{D_{\alpha}^{(i)}, \alpha \in K = \{1, \dots, s_i\}\}$, that are necessary for implementation of BP $A_i, i = 1, \dots, n$. Let $B = \{B_j, j \in M = \{1, \dots, m\}\}$ be a set VE main elements and subsystems. Each element B_j can include technical facilities $C^{(j)} = \{C_{\lambda}^{(j)}, \lambda \in L = \{1, \dots, l_j\}\}$ with

appropriate computer equipment and software. Technical facilities are used for implementation of control functions.

Let $E(t) = \|e_{ij}(t)\|$ be a known matrix function, with $e_{ij}(t)=1$ in case of the subsystem B_j is carrying out the function A_i at time t in accordance with time-spatial, technical and technological constraints, $e_{ij}(t)=0$ otherwise.

Fig.1 presents an example of seven possible structural states of IIS. The arrows show variants of communication within the system. These variants correspond to different control technologies (methods of IIS application) and different spatial structures of VE.

Now the verbal description of a functions-distribution problem can be presented as follows. It is necessary to select the best variants of functions distribution among the nodes of IIS for each structural state R_1, R_2, \dots, R_k of IIS (under known time spatial, technical and technological constraints) and to find the best variants of functions implementation. The structural states of IIS should be sorted according to their preference. The preference relation can be expressed through quality functions characterizing efficiency of IIS and its structural and technologic characteristics.

The described problem belongs to the class of multi-criteria choice problems with finite sets of alternatives (structural states of IIS).

ALGORITHM OF MULTI-CRITERIA PLANNING OPERATIONS IN IIS

The general algorithm for the problem includes the following steps.

Step 1. Models (analytical, simulation and combined models) describing structural states R_1, R_2, \dots, R_k are used for optimal distribution of BP and control functions among subsystems of IIS, for technological operations planning and for evaluation of IIS efficiency. The following characteristics of IIS efficiency can be used: the total number of functions implemented in subsystems during the interval T, the total number of BP in given macro-states, the total number of technological operations executed over the time interval T, the total time of operations over the time period T. The above-mentioned characteristics can have stochastic or fuzzy interpretation if uncertainty factors are present (Okhtilev et al 2006, Orlovski. 1981).

The following dynamic model of functions distribution can be used for evaluation of IIS efficiency (Okhtilev et al 2006, Kalinin and Sokolov 1995, Zimin and Ivanilov 1971).

$$\begin{aligned} \dot{x}_i^{(\phi)} &= \sum_{j=1}^m \varepsilon_{ij}(t) u_{ij}^{(\phi)}, \quad \dot{x}_{i\alpha j}^{(0)} = \sum_{\lambda=1}^l b_{i\alpha j\lambda} u_{i\alpha j\lambda}^{(0)}, \\ \dot{y}_{ij}^{(\phi)} &= v_{ij}^{(\phi)}; \end{aligned} \quad (1)$$

$$\sum_{j=1}^m u_{ij}^{(\phi)} \left[\sum_{\alpha \in \Gamma_{i1}} (a_\alpha^{(\phi)} - x_\alpha^{(\phi)}) + \prod_{\beta \in \Gamma_{i2}} (a_\beta^{(\phi)} - x_\beta^{(\phi)}) \right] = 0; \quad (2)$$

$$\sum_{\lambda=1}^l u_{i\alpha j\lambda}^{(0)} \left[\sum_{v \in \Gamma_{i\alpha 1}} (a_{iv}^{(0)} - x_{iv}^{(0)}) + \prod_{\mu \in \Gamma_{i\alpha 2}} (a_{i\mu}^{(0)} - x_{i\mu}^{(0)}) \right] = 0; \quad (3)$$

$$\begin{aligned} \sum_{i=1}^n u_{ij}^{(\phi)}(t) &\leq 1; \quad \forall j; \quad \sum_{j=1}^m u_{ij}^{(\phi)}(t) \leq 1; \quad \forall i; \\ u_{ij}^{(\phi)}(t) &\in \{0, 1\}; \end{aligned} \quad (4)$$

$$\begin{aligned} \sum_{j=1}^m \sum_{\lambda=1}^l u_{i\alpha j\lambda}^{(0)}(t) &\leq 1, \quad \forall i, \forall \alpha; \quad \sum_{i=1}^n \sum_{\alpha=1}^s u_{i\alpha j\lambda}^{(0)}(t) \leq 1, \\ \forall i, \forall \alpha; \quad u_{i\alpha j\lambda}^{(0)}(t) &\in \{0, u_{ij}^{(\phi)}\}; \end{aligned} \quad (5)$$

$$v_{ij}^{(\phi)}(a_{isj}^{(0)} - x_{isj}^{(0)}) = 0; \quad v_{ij}^{(\phi)}(t) \in \{0, 1\}; \quad (6)$$

$$x_i^{(\phi)}(t_0) = x_{i\alpha j}^{(0)}(t_0) = y_{ij}^{(\phi)}(t_0) = 0; \quad (7)$$

$$\begin{aligned} x_i^{(\phi)}(t_f) &= a_i^{(\phi)}; \quad (a_{i\alpha j}^{(0)} - x_{i\alpha j}(t_f)) y_{ij}^{(\phi)}(t_f) = 0; \\ x_i^{(\phi)}(t_f) &= a_i^{(\phi)}; \quad (a_{i\alpha j}^{(0)} - x_{i\alpha j}(t_f)) y_{ij}^{(\phi)}(t_f) = 0; \end{aligned} \quad (8)$$

$$\begin{aligned} J_0 &= \sum_{i=1}^n \sum_{j=1}^m v_{ij}^{(\phi)}(t_f); \quad J_1^{(n)} = \sum_{i=1}^m v_{nj}^{(\phi)}(t_f); \\ J_0 &= \sum_{i=1}^n \sum_{j=1}^m v_{ij}^{(\phi)}(t_f); \quad J_1^{(n)} = \sum_{i=1}^m v_{nj}^{(\phi)}(t_f); \end{aligned} \quad (9)$$

where $x_i^{(\phi)}(t)$ is equal to total duration of the business process A_i fulfillment in subsystem B_j as $u_{ij}^{(\phi)}(t) = 1$; the variable $x_{i\alpha j}^{(0)}$ express the current state of the technological operation $D_{\alpha}^{(i)}$; $y_{ij}^{(\phi)}$ is equal to the time passed after A_i completion in B_j until the time $t = t_f$; $a_\alpha^{(\phi)}, a_\alpha^{(0)}, a_\gamma^{(0)}, a_{ivj}^{(0)}, a_{i\mu j}^{(0)}$ are given values setting end conditions for $x_i^{(\phi)}(t), x_\alpha^{(\phi)}(t), x_\gamma^{(\phi)}(t), x_{ivj}^{(0)}(t), x_{i\mu j}^{(0)}(t)$ at time $t = t_f$; $u_{ij}^{(\phi)}, u_{i\alpha j\lambda}^{(0)}, v_{ij}^{(\phi)}$ are control inputs. Here $u_{ij}^{(\phi)}(t) = 1$ if BP A_i is being executed in the subsystem B_j at time t , $u_{ij}^{(\phi)}(t) = 0$ otherwise; $u_{i\alpha j\lambda}^{(0)}(t) = 1$ if the technological operation $D_{\alpha}^{(i)}$ is executed in the technical facility $C_\lambda^{(j)}$, $u_{i\alpha j\lambda}^{(0)}(t) = 0$ otherwise; $v_{ij}^{(\phi)} = 1$ if BP A_i was implemented in the subsystem B_j , $v_{ij}^{(\phi)} = 0$ otherwise.

Here the sets Γ_{i1}, Γ_{i2} include the numbers of functions that are direct predecessors of the control function A_i . The set Γ_{i1} indicates predecessors connected by logical "and", the set Γ_{i2} indicates

predecessors connected by logical “or”. The sets $\Gamma_{i \in 1}$, $\Gamma_{i \in 2}$ include the numbers of technological operations $D_v^{(i)}$ and $D_\mu^{(i)}$ that are direct predecessors of the operation $D_\alpha^{(i)}$. The subscripts 1 and 2 express the type of logical connection as stated above.

Therefore, constraints (2) and (3) define allowable sequences of control functions and technological operations. Constraints (4) and (5) specify that each BP at each time can be carried out only in one subsystem B_j ($i=1, \dots, n; j=1, \dots, m$) and conversely, each subsystem B_j can carry out only one BP A_i at the same time. Similar constraints are used for technological operations $D_\alpha^{(i)}$ that are executed at the technical facility $C_\lambda^{(j)}$.

Expression (6) states switching-on conditions for the auxiliary control input $v_{ij}^{(\phi)}(t)$. Expressions (7) and (8) specify end conditions for the state variables at the time $t = t_0$, $t = t_f$, R^1 is a set of positive real numbers. The functionals J_0, J_1, J_2 are quality measures for distribution of BP in IIS. Here J_0 is equal to total number of functions by the time $t = t_f$, J_1 is equal to the number of subsystems the function A_i is implemented in, J_2 expresses the elapsed time for implementation of all necessary functions.

A simulation model of real-time control can be used together with expressions (1)-(9) for taking into account uncertainty factors. In this case special procedures of inter-model coordination can be used (Okhtilev et al 2006, Kalinin and Sokolov 1995).

Extreme values of functionals characterizing IIS efficiency can be determined via solution of optimal control problem for finite-dimensional differential system with mixed conditions. The solution algorithms and different aspects of their programming are considered in (Okhtilev et al 2006, Kalinin and Sokolov 1995).

Step 2. Structure-topological characteristics of IIS are being evaluated (Zimin and Ivanilov 1971) including: the coefficient of attainability J_4 , different measures of structure compactness (radius J_5 of the structure, diameter J_6 of the structure, integral measure J_7 of structural compactness), measures J_8 of structure centralization (decentralization).

The formulas for computation of measures are proposed in (Zimin and Ivanilov 1971).

Step 3. The pairwise-comparison matrix Kc is completed for measuring the IIS efficiency. Expert appraisal is used for completion of the matrix.

Step 4. The weights of measures (significance coefficients) are evaluated according to the matrix Kc . The algorithm proposed in (Orlovski 1981) is used here. The vector of coefficients is equal to the normalized eigenvector $\vec{\omega}_c$ corresponding to the maximal eigenvalue $Lmax$ of the matrix Kc . Thus the following equation has to be solved:

$$(Kc - Lmax * I) \vec{\omega}_c = 0, \quad (10)$$

where I is a unitary matrix.

Then a weight of each structural state (R_1, R_2, \dots, R_k) of IIS for each measure taken separately is evaluated. These weights complete the matrix Kr . Each column of the matrix Kr includes relative weights of the states in respect of some measure. A weighted sum of measures is received for each alternative R_1, R_2, \dots, R_k . In other words, total sets of weights are determined for each structural state via the formula:

$$Kr \vec{\omega}_c = \vec{\omega}^*. \quad (11)$$

Step 5. The structural states are sorted according to their preference. The best one is characterized with the maximal element of the vector $\vec{\omega}^*$. Each element of the vector $\vec{\omega}^*$ can be interpreted as a total weight of some structural state.

CONCLUSIONS

Dynamic interpretation of operation planning in IIS let thoroughly describe and investigate interrelation and interaction of business processes and the processes of information processing, storing and interchange.

The framework of integrated multi-criteria operations planning in the context of IIS structure-dynamics control results in the following advantages. The goals of IIS planning can be directly interrelated with the goals of business processes. Structure-dynamics operations (IIS control technology) can be reasonably selected and substantiated. Efficient compromise solutions can be found for allocation of control functions among the elements of IIS and for general programs (plans) of IIS operation. The preliminary ordering of IIS structural states let rapidly reconfigure it in case of failures (Okhtilev et al 2006).

Several prototype versions of software were produced for structure-dynamics control of IIS in different application domains (cosmonautics, power industry, management, etc, see <http://www.spiiras-grom.ru>). The experiments with software confirmed efficiency of models applied.

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